



# Moments of Inertia

## Uninhabited Aerial Vehicle (UAV) Dryden Remotely Operated Integrated Drone (DROID)



Presented by Helida C. Haro  
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# Agenda

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- ! **Personal Background**

- ! **Research**

- ! **Importance**
- ! **Measure, Weight, CG**
- ! **Design Hardware and Test**
- ! **Machining**
- ! **Hangar**
- ! **Safety Mitigations**
- ! **Critical Design Review (CDR)**
- ! **Tech Brief**
- ! **Test**
- ! **Analyze Data**

- ! **Lessons Learned**

- ! **Future Plans**

- ! **Questions**









# Research



Figure 7, include the lengths of the vertical threads and the distance between the parallel bifilar. The inertia of the mounting





# Mass Properties

The mass properties of an object are simply the proportionality constants between applied force and the resulting acceleration:

$$f = m\ddot{x}$$

$$T = j\alpha$$

This is Newton's 2nd law for 1 Degree of Freedom (DOF) translation and rotation, respectively

When expanded to 6 DOF:

$$\begin{matrix} \text{Mass} \\ \text{6 DOF} \\ \text{force} \end{matrix} \begin{bmatrix} F_x \\ F_y \\ F_z \\ M_x \\ M_y \\ M_z \end{bmatrix}_P = \begin{bmatrix} m & 0 & 0 & 0 & 0 & 0 \\ 0 & m & 0 & -mZ_{CG} & mY_{CG} & 0 \\ 0 & 0 & m & mY_{CG} & -mX_{CG} & 0 \\ 0 & -mZ_{CG} & mY_{CG} & I_{xx} & -I_{xy} & -I_{xz} \\ mZ_{CG} & 0 & -mX_{CG} & -I_{yx} & I_{yy} & -I_{yz} \\ -mY_{CG} & mX_{CG} & 0 & -I_{zx} & -I_{zy} & I_{zz} \end{bmatrix} \begin{bmatrix} \ddot{x} \\ \ddot{y} \\ \ddot{z} \\ \ddot{\theta}_x \\ \ddot{\theta}_y \\ \ddot{\theta}_z \end{bmatrix}_P$$

CG information

Inertia Tensor

6 DOF acceleration





# Importance

The inertial characteristics have direct !  
consequences on:!

Aerodynamics !

! ! ! Propulsion!

! ! ! Structures!

! ! ! Control!





# Measure and Weight



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# Design



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# Shuttle Hangar



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# Safety

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- **! Human Hazard Analysis**
- **! Loss of Asset/Mission Hazard Analysis**





# Approvals

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- **! Critical Design Review (CDR)**
- **! Tech Brief**

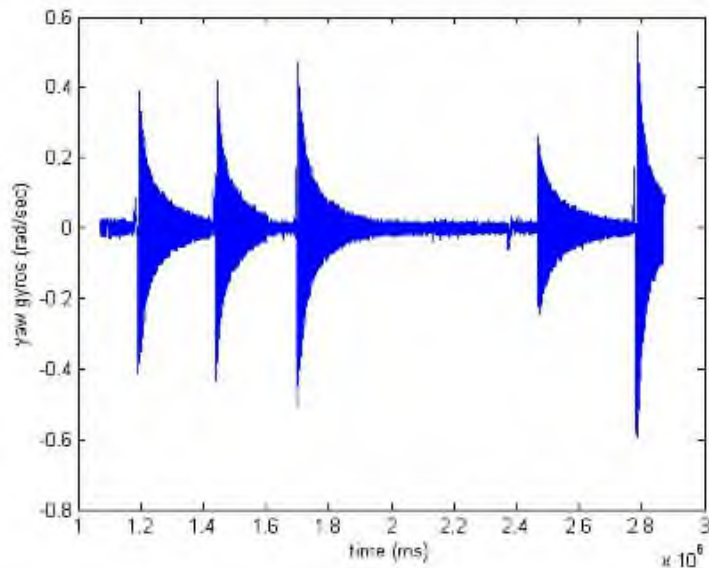








# Data Analysis



- **! Time Constraints**
- **! Basic Geometric Shapes**
- **! MATLAB**
- **! Error**

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# Lessons Learned

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- **!Dryden vs. Disneyland**
- **!Learning**
- **!Team Effort**
- **!Double check all work**
- **!Stress Testing**
- **!Use steel instead of aluminum**





## Future Plans

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- **!GSRP at NASA Headquarters**
- **!Graduate**
- **!Work for NASA**







# Questions?



Mark, Chris, Aaron, Lesli, Stephanie, Alex, and Helida!

All photos provided by: NASA photographer, Thomas P. Tschida and INSPIRE Team!

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## BACK-UP: Inertia Calculations

$$I_{Pod} = \left( \frac{g}{16\pi^2} \right) \left( \frac{d^2}{l} \right) T^2 (W_{Pod} + W_{Rig}) - I_{Rig}$$

Where,

**I** = Yaw Mass Moment of Inertia, [lb-in<sup>2</sup>]

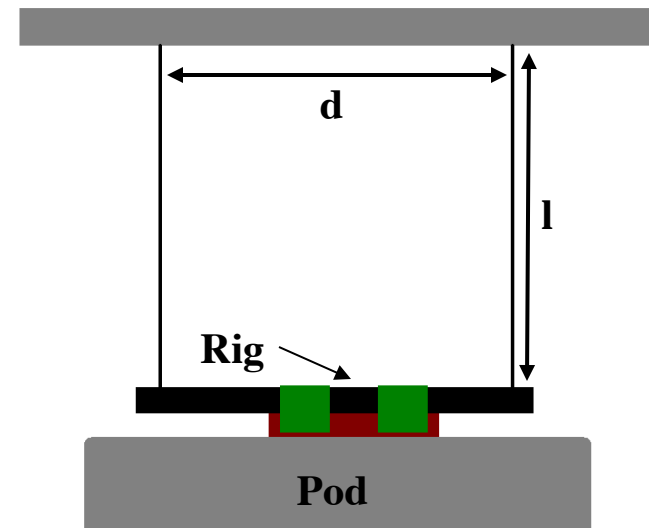
**g** = gravity, [in/sec<sup>2</sup>]

**d** = Distance Between Cables, [in]

**l** = Cable Length, [in]

**T** = Period of Oscillation, [sec]

**W** = Weight, [lb]



Reference:

NACA TN No.351

